

Package ‘modifiedmk’

June 10, 2021

Title Modified Versions of Mann Kendall and Spearman's Rho Trend Tests

Version 1.6

Description Power of non-parametric Mann-Kendall test and Spearman's Rho test is highly influenced by serially correlated data. To address this issue, trend tests may be applied on the modified versions of the time series data by Block Bootstrapping (BBS), Prewhitening (PW), Trend Free Prewhitening (TFPW), Bias Corrected Prewhitening and Variance Correction Approach by calculating effective sample size.

Mann, H. B. (1945).<[doi:10.1017/CBO9781107415324.004](https://doi.org/10.1017/CBO9781107415324.004)>.

Kendall, M. (1975). Multivariate analysis. Charles Griffin&Company Ltd.,
sen, P. K. (1968).<[doi:10.2307/2285891](https://doi.org/10.2307/2285891)>.

Önöz, B., & Bayazit, M. (2012) <[doi:10.1002/hyp.8438](https://doi.org/10.1002/hyp.8438)>.

Hamed, K. H. (2009).<[doi:10.1016/j.jhydrol.2009.01.040](https://doi.org/10.1016/j.jhydrol.2009.01.040)>.

Yue, S., & Wang, C. Y. (2002) <[doi:10.1029/2001WR000861](https://doi.org/10.1029/2001WR000861)>.

Yue, S., Pilon, P., Phinney, B., & Cavadias, G. (2002) <[doi:10.1002/hyp.1095](https://doi.org/10.1002/hyp.1095)>.

Hamed, K. H., & Ramachandra Rao, A. (1998) <[doi:10.1016/S0022-1694\(97\)00125-X](https://doi.org/10.1016/S0022-1694(97)00125-X)>.

Yue, S., & Wang, C. Y. (2004) <[doi:10.1023/B:WARM.0000043140.61082.60](https://doi.org/10.1023/B:WARM.0000043140.61082.60)>.

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R topics documented:

bbsmk	2
bbssr	3
bcpw	5
mkttest	6
mmkh	7
mmkh3lag	9
mmky	10
mmky1lag	11
pbnk	13
pwmk	14
spear	15
tfpwmk	16
x	17

Index	19
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bbsmk	<i>Nonparametric Block Bootstrapped Mann-Kendall Trend Test</i>
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Description

Significant serial correlation present in time series data can be accounted for using the nonparametric block bootstrap technique, which incorporates the Mann-Kendall trend test (Mann, 1945; Kendall, 1975; Kundzewicz and Robson, 2000). Predetermined block lengths are used in resampling the original time series, thus retaining the memory structure of the data. If the value of the test statistic falls in the tails of the empirical bootstrapped distribution, there is likely a trend in the data. The block bootstrap technique is powerful in the presence of autocorrelation (Khaliq et al. 2009; Önöz and Bayazit, 2012).

Usage

```
bbsmk(x, ci=0.95, nsim=2000, eta=1, bl.len=NULL)
```

Arguments

x	- Time series data vector
ci	- Confidence interval
nsim	- Number of bootstrapped simulations
eta	- Added to the block length
bl.len	- Block length

Details

Block lengths are automatically selected using the number of contiguous significant serial correlations, to which the eta (η) term is added. A value of $\eta = 1$ is used as the default as per Khaliq et al. (2009). Alternatively, the user may define the block length. 2000 bootstrap replicates are recommended as per Svensson et al. (2005) and Önöz, B. and Bayazit (2012).

Value

Z-Value - Mann-Kendall Z statistic

Sen's slope - Sen's trend slope

S - Mann-Kendall S statistic

Tau - Mann-Kendall's Tau value

Kendall's Tau Empirical Bootstrapped CI - Kendall's Tau empirical bootstrapped confidence interval

Z-value Empirical Bootstrapped CI - Z-value empirical bootstrapped confidence interval

References

Box, G. E. P. and Jenkins, G. M. (1970). Time Series Analysis Forecasting and Control. Holden-Day, San Francisco, California, 712 pp.

Kendall, M. (1975). Rank Correlation Methods. Griffin, London, 202 pp.

Khaliq, M. N., Ouarda, T. B. M. J., Gachon, P., Sushama, L., and St-Hilaire, A. (2009). Identification of hydrological trends in the presence of serial and cross correlations: A review of selected methods and their application to annual flow regimes of Canadian rivers. *Journal of Hydrology*, 368: 117-130.

Kundzewicz, Z. W. and Robson, A. J. (2000). Detecting Trend and Other Changes in Hydrological Data. World Climate Program-Data and Monitoring. World Meteorological Organization, Geneva (WMO/TD-No. 1013).

Kundzewicz, Z. W. and Robson, A. J. (2004). Change detection in hydrological records-A review of the methodology. *Hydrological Sciences Journal*, 49(1): 7-19.

Mann, H. B. (1945). Nonparametric Tests Against Trend. *Econometrica*, 13(3): 245-259.

Önöz, B. and Bayazit M. (2012). Block bootstrap for Mann-Kendall trend test of serially dependent data. *Hydrological Processes*, 26: 3552-3560.

Svensson, C., Kundzewicz, Z. W., and Maurer, T. (2005). Trend detection in river flow series: 2. Floods and low-flow index series. *Hydrological Sciences Journal*, 50(5): 811-823.

Examples

```
x<-c(Nile[1:10])  
bbsmk(x)
```

Description

Significant serial correlation present in time series data can be accounted for using the nonparametric block bootstrap technique, which incorporates Spearman's Rank Correlation trend test (Lehmann, 1975; Sneyers, 1990; Kundzewicz and Robson, 2000). Predetermined block lengths are used in resampling the original time series, thus retaining the memory structure of the data. If the value of the test statistic falls in the tails of the empirical bootstrapped distribution, there is likely a trend in the data. The block bootstrap technique is powerful in the presence of autocorrelation (Khaliq et al. 2009; Önöz and Bayazit, 2012).

Usage

```
bbssr(x, ci=0.95, nsim=2000, eta=1, bl.len=NULL)
```

Arguments

x	- Time series data vector
ci	- Confidence interval
nsim	- Number of bootstrapped simulations
eta	- Added to the block length
bl.len	- Block length

Details

Block lengths are the number of contiguous significant serial correlations, to which the (η) term is added. A value of $\eta = 1$ is used as the default as per Khaliq et al. (2009). Alternatively, the user may define the block length. 2000 bootstrap replicates are recommended as per Svensson et al. (2005) and Önöz, B. and Bayazit (2012).

Value

Spearman's Correlation Coefficient - Spearman's correlation coefficient value

Test Statistic - Z-transformed value to test significance $\rho(\sqrt{n-1})$

Test Statistic Empirical Bootstrapped CI - Test statistic empirical bootstrapped confidence interval

References

- Box, G. E. P. and Jenkins, G. M. (1970). Time Series Analysis Forecasting and Control. Holden-Day, San Fransisco, California, 712 pp.
- Khaliq, M. N., Ouarda, T. B. M. J., Gachon, P., Sushama, L., and St-Hilaire, A. (2009). Identification of hydrological trends in the presence of serial and cross correlations: A review of selected methods and their application to annual flow regimes of Canadian rivers. *Journal of Hydrology*, 368: 117-130.
- Kundzewicz, Z. W. and Robson, A. J. (2000). Detecting Trend and Other Changes in Hydrological Data. World Climate Program-Water, Data and Monitoring. World Meteorological Organization, Geneva (WMO/TD-No. 1013).

Kundzewicz, Z. W. and Robson, A. J. (2004). Change detection in hydrological records-A review of the methodology. *Hydrological Sciences Journal*, 49(1): 7-19.

Lehmann, E. L. (1975). *Nonparametrics: statistical methods based on ranks*. Holden-Day, Inc., California, 457 pp.

Önöz, B. and Bayazit M. (2012). Block bootstrap for Mann-Kendall trend test of serially dependent data. *Hydrological Processes*, 26: 3552-3560.

Sneyers, R. (1990). On the statistical analysis of series of observations. World Meteorological Organization, Technical Note no. 143, WMO no. 415, 192 pp.

Svensson, C., Kundzewicz, Z. W., and Maurer, T. (2005). Trend detection in river flow series: 2. Floods and low-flow index series. *Hydrological Sciences Journal*, 50(5): 811-823.

Examples

```
x<-c(Nile[1:10])
bbssr(x)
```

bcpw

Hamed (2009) Bias Corrected Prewhitening.

Description

Hamed (2009) proposed a prewhitening technique in which the slope and lag-1 serial correlation coefficient are simultaneously estimated. The lag-1 serial correlation coefficient is then corrected for bias before prewhitening.

Usage

```
bcpw(x)
```

Arguments

x - Time series data vector

Details

Employs ordinary least squares (OLS) to simultaneously estimate the lag-1 serial correlation coefficient and slope of trend. The lag-1 serial correlation coefficient is then bias corrected.

Value

Z-Value - Mann-Kendall Z-statistic after bias corrected prewhitening

Prewhitened Sen's Slope - Sen's slope of the prewhitened data

Sen's Slope - Sen's slope for the original data series 'x'

P-value - p-value after prewhitening

S - Mann-Kendall 'S' statistic
Var(s) - Variance of 'S'
Tau - Mann-Kendall's Tau

References

Hamed, K. H. (2009). Enhancing the effectiveness of prewhitening in trend analysis of hydrologic data. *Journal of Hydrology*, 368: 143-155.

Kendall, M. (1975). *Multivariate analysis*. Charles Griffin. Londres. 0-85264-234-2.

Mann, H. B. (1945). Nonparametric Tests Against Trend. *Econometrica*, 13(3), 245-259. <doi:10.1017/CBO9781107415324>

van Giersbergen, N. P. A. (2005). On the effect of deterministic terms on the bias in stable AR models. *Economic Letters*, 89: 75-82.

Examples

```
x<-c(Nile)
bcpw(x)
```

mkttest

Mann-Kendall Trend Test of Time Series Data Without Modifications

Description

The Mann-Kendall trend test is a nonparametric trend test used to identify monotonic trends present in time series data.

Usage

```
mkttest(x)
```

Arguments

x - Time series data vector

Details

The Mann-Kendall trend test is a nonparametric trend tests which assumes no distribution of the data. The null hypothesis of the test is that there is no trend in the data and the alternative hypothesis is that the data represents a monotonic trend.

Value

Z - Mann-Kendall Z statistic
Sen's slope - Sen's slope
S - Mann-Kendall S statistic
Var(s) - Variance of S
P-value - Mann-Kendall p-value
Tau - Mann-Kendall's Tau

References

Kendall, M. (1975). Rank Correlation Methods. Griffin, London, 202 pp.
Mann, H. B. (1945). Nonparametric Tests Against Trend. *Econometrica*, 13(3): 245-259.
Sen, P. K. (1968). Estimates of the Regression Coefficient Based on Kendall's Tau. *Journal of the American statistical Association*, 63(324): 1379. <doi:10.2307/2285891>

Examples

```
x<-c(Nile)
mkttest(x)
```

mmkh

Modified Mann-Kendall Test For Serially Correlated Data Using the Hamed and Rao (1998) Variance Correction Approach

Description

Time series data is often influenced by previous observations. When data is not random and influenced by autocorrelation, modified Mann-Kendall tests may be used for trend detection studies. Hamed and Rao (1998) have proposed a variance correction approach to address the issue of serial correlation in trend analysis. Data are initially detrended and the effective sample size is calculated using the ranks of significant serial correlation coefficients which are then used to correct the inflated (or deflated) variance of the test statistic.

Usage

```
mmkh(x, ci=0.95)
```

Arguments

x - Time series data vector
ci - Confidence interval

Details

A detrended time series is constructed using Sen's slope and the lag-1 autocorrelation coefficient of the ranks of the data. The variance correction approach proposed by Hamed and Rao (1998) uses only significant lags of autocorrelation coefficients.

Value

Corrected Zc - Z statistic after variance Correction

new P.value - P-value after variance correction

N/N* - Effective sample size

Original Z - Original Mann-Kendall Z statistic

Old P-value - Original Mann-Kendall p-value

Tau - Mann-Kendall's Tau

Sen's Slope - Sen's slope

old.variance - Old variance before variance Correction

new.variance - Variance after correction

References

Hamed, K. H. and Rao, A. R. (1998). A modified Mann-Kendall trend test for autocorrelated data. *Journal of Hydrology*, 204(1-4): 182-196. <doi:10.1016/S0022-1694(97)00125-X>

Kendall, M. (1975). *Rank Correlation Methods*. Griffin, London, 202 pp.

Mann, H. B. (1945). Nonparametric Tests Against Trend. *Econometrica*, 13(3): 245-259.

Rao, A. R., Hamed, K. H., & Chen, H.-L. (2003). *Nonstationarities in hydrologic and environmental time series*. Ringgold Inc., Portland, Oregon, 362 pp. <doi:10.1007/978-94-010-0117-5>

Salas, J.D. (1980). *Applied modeling of hydrologic times series*. Water Resources Publication, 484 pp.

Sen, P. K. (1968). Estimates of the Regression Coefficient Based on Kendall's Tau. *Journal of the American statistical Association*, 63(324): 1379. <doi:10.2307/2285891>

Examples

```
x<-c(Nile)
mmkh(x)
```

mmkh3lag	<i>Modified Mann-Kendall Test For Serially Correlated Data Using the Hamed and Rao (1998) Variance Correction Approach Considering Only the First Three Lags</i>
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Description

Time series data is often influenced by serial correlation. When data are not random and influenced by autocorrelation, modified Mann-Kendall tests may be used for trend detection. Hamed and Rao (1998) have proposed variance correction approach to address the issue of serial correlation in Trend analysis. Data are initially detrended and the effective sample size is calculated using the ranks of significant serial correlation coefficients which are then used to correct the inflated (or deflated) variance of the test statistic.

Usage

```
mmkh3lag(x, ci=0.95)
```

Arguments

x	- Time series data vector
ci	- Confidence interval

Details

A detrended time series is constructed using Sen's slope and the lag-1 autocorrelation coefficient of the ranks of the data. The variance correction approach proposed by Hamed and Rao (1998) uses only significant lags of autocorrelation coefficients. As suggested by Rao et al. (2003), only the first three autocorrelation coefficients are used in this function.

Value

Corrected Zc - Z statistic after variance Correction
 new P.value - P-value after variance correction
 N/N* - Effective sample size
 Original Z - Original Mann-Kendall Z statistic
 Old P-value - Original Mann-Kendall p-value
 Tau - Mann-Kendall's Tau
 Sen's Slope - Sen's slope
 old.variance - Old variance before variance Correction
 new.variance - Variance after correction

References

- Hamed, K. H. and Rao, A. R. (1998). A modified Mann-Kendall trend test for autocorrelated data. *Journal of Hydrology*, 204(1–4): 182–196. <doi:10.1016/S0022-1694(97)00125-X>.
- Kendall, M. (1975). *Rank Correlation Methods*. Griffin, London, 202 pp.
- Mann, H. B. (1945). Nonparametric Tests Against Trend. *Econometrica*, 13(3): 245-259.
- Rao, A. R., Hamed, K. H., & Chen, H.-L. (2003). *Nonstationarities in hydrologic and environmental time series*. Ringgold Inc., Portland, Oregon, 362 pp. <doi:10.1007/978-94-010-0117-5>
- Salas, J.D. (1980). *Applied modeling of hydrologic times series*. Water Resources Publication, 484 pp.
- Sen, P. K. (1968). Estimates of the Regression Coefficient Based on Kendall's Tau. *Journal of the American statistical Association*, 63(324): 1379. <doi:10.2307/2285891>

Examples

```
x<-c(Nile)
mmkh3lag(x)
```

mmky

Modified Mann-Kendall Test For Serially Correlated Data Using the Yue and Wang (2004) Variance Correction Approach

Description

Time series data is often influenced by serial correlation. When data are not random and influenced by autocorrelation, modified Mann-Kendall tests may be used for trend detection. Yue and Wang (2004) have proposed variance correction approach to address the issue of serial correlation in trend analysis. Data are initially detrended and the effective sample size is calculated using significant serial correlation coefficients.

Usage

```
mmky(x)
```

Arguments

x - Time series data vector

Details

The variance correction approach suggested by Yue and Wang (2004) is implemented in this function. Serial correlation coefficients for all lags are used in calculating the effective sample size.

Value

Corrected Zc - Z statistic after variance Correction

new P.value - P-value after variance correction

N/N* - Effective sample size

Original Z - Original Mann-Kendall Z statistic

Old P-value - Original Mann-Kendall p-value

Tau - Mann-Kendall's Tau

Sen's Slope - Sen's slope

old.variance - Old variance before variance Correction

new.variance - Variance after correction

References

Kendall, M. (1975). Rank Correlation Methods. Griffin, London, 202 pp.

Mann, H. B. (1945). Nonparametric Tests Against Trend. *Econometrica*, 13(3): 245-259.

Sen, P. K. (1968). Estimates of the Regression Coefficient Based on Kendall's Tau. *Journal of the American statistical Association*, 63(324): 1379. <doi:10.2307/2285891>

Yue, S. and Wang, C. Y. (2004). The Mann-Kendall test modified by effective sample size to detect trend in serially correlated hydrological series. *Water Resources Management*, 18(3): 201–218. <doi:10.1023/B:WARM.0000043140.61082.60>

Examples

```
x<-c(Nile)
mmky(x)
```

mmky1lag

Modified Mann-Kendall Test For Serially Correlated Data Using the Yue and Wang (2004) Variance Correction Approach Using the Lag-1 Correlation Coefficient Only

Description

Time series data is often influenced by serial correlation. When data are not random and influenced by autocorrelation, modified Mann-Kendall tests may be used for trend detection. Yue and Wang (2004) have proposed a variance correction approach to address the issue of serial correlation in trend analysis. Data are initially detrended and the effective sample size is calculated using the lag-1 autocorrelation coefficient.

Usage

```
mmky1lag(x)
```

Arguments

x - Time series data vector

Details

The variance correction approach suggested by Yue and Wang (2004) is implemented in this function. Effective sample size is calculated based on the AR(1) assumption.

Value

Corrected Zc - Z statistic after variance Correction

new P.value - P-value after variance correction

N/N* - Effective sample size

Original Z - Original Mann-Kendall Z statistic

Old P-value - Original Mann-Kendall p-value

Tau - Mann-Kendall's Tau

Sen's Slope - Sen's slope

old.variance - Old variance before variance Correction

new.variance - Variance after correction

References

Kendall, M. (1975). Rank Correlation Methods. Griffin, London, 202 pp.

Mann, H. B. (1945). Nonparametric Tests Against Trend. *Econometrica*, 13(3): 245-259.

Sen, P. K. (1968). Estimates of the Regression Coefficient Based on Kendall's Tau. *Journal of the American statistical Association*, 63(324): 1379. <doi:10.2307/2285891>

Yue, S. and Wang, C. Y. (2004). The Mann-Kendall test modified by effective sample size to detect trend in serially correlated hydrological series. *Water Resources Management*, 18(3): 201–218. <doi:10.1023/B:WARM.0000043140.61082.60>

Examples

```
x<-c(Nile)
mmky1lag(x)
```

pbmk *Bootstrapped Mann-Kendall Trend Test with Optional Bias Corrected Prewhitening*

Description

The empirical distribution of the Mann-Kendall test statistic is calculated by bootstrapped resampling. The Hamed (2009) bias correction prewhitening technique can optionally be applied as the default for prewhitening before the bootstrapped Mann-Kendall test is applied (Lacombe et al., 2012).

Usage

```
pbmk(x, nsim=1000, pw="Hamed")
```

Arguments

x - Time series data vector
 nsim - Number of bootstrapped simulations
 pw - Optional bias corrected prewhitening suggested by Hamed (2009)

Details

Bootstrapped samples are calculated by resampling one value at a time from the time series with replacement. The p-value (p_s) of the resampled data is estimated by (Yue and Pilon, 2004):

$$p_s = m_s/M$$

The Mann-Kendall test statistics (S) is calculated for each resampled dataset. The resultant vector of resampled S statistics is then sorted in ascending ordering, where p_s is the rank corresponding the largest bootstrapped value of S being less than the test statistic value calculated from the actual data. M is the total number of bootstrapped resamples. The default value of M is 1000, however, Yue and Pilon (2004) suggest values between 1000 and 2000. If the user does not choose to apply prewhitening, this argument 'pw' can be set to NULL.

Value

Z Value - Mann-Kendall Z statistic from original data
 Sen's Slope - Sen's slope from the original data
 S - Mann-Kendall S statistic
 Kendall's Tau - Mann-Kendall's Tau
 BCP Z Value - Bias corrected prewhitened Z value
 BCP Sen's Slope - Bias corrected prewhitened Sen's slope
 BCP S - Bias corrected prewhitened S
 BCP Kendall's Tau - Bias corrected prewhitened Kendall's Tau
 Bootstrapped P-Value - Mann-Kendall bootstrapped p-value

References

- Hamed, K. H. (2009). Enhancing the effectiveness of prewhitening in trend analysis of hydrologic data. *Journal of Hydrology*, 368: 143-155.
- Kendall, M. (1975). *Rank Correlation Methods*. Griffin, London, 202 pp.
- Kundzewicz, Z. W. and Robson, A. J. (2004). Change detection in hydrological records - a review of the methodology. *Hydrological Sciences Journal*, 49(1): 7-19.
- Lancombe, G., McCartney, M., and Forkuor, G. (2012). Drying climate in Ghana over the period 1960-2005: evidence from the resampling-based Mann-Kendall test at local and regional levels. *Hydrological Sciences Journal*, 57(8): 1594-1609.
- Mann, H. B. (1945). Nonparametric Tests Against Trend. *Econometrica*, 13(3): 245-259.
- van Giersbergen, N. P. A. (2005). On the effect of deterministic terms on the bias in stable AR models. *Economic Letters*, 89: 75-82.
- Yue, S. and Pilon, P. (2004). A comparison of the power of the t test, Mann-Kendall and bootstrap tests for trend detection, *Hydrological Sciences Journal*, 49(1): 21-37.

Examples

```
x<-c(Nile[1:10])
pbmk(x)
```

pwmk

Mann-Kendall Test of Prewhitened Time Series Data in Presence of Serial Correlation Using the von Storch (1995) Approach

Description

When time series data are not random and influenced by autocorrelation, prewhitening the time series prior to application of trend test is suggested.

Usage

```
pwmk(x)
```

Arguments

x - Time series data vector

Details

The lag-1 serial correlation coefficient is used for prewhitening.

Value

Z-Value - Z statistic after prewhitening
 Sen's Slope - Sen's slope for prewhitened series
 old. Sen's Slope - Sen's slope for original data series (x)
 P-value - P-value after prewhitening
 S - Mann-Kendall S statistic
 Var(s) - Variance of S
 Tau - Mann-Kendall's Tau

References

Kendall, M. (1975). Rank Correlation Methods. Griffin, London, 202 pp.
 Kulkarni, A. and H. von Storch. 1995. Monte carlo experiments on the effects of serial correlation on the MannKendall test of trends. Meteorologische Zeitschrift N.F, 4(2): 82-85.
 Mann, H. B. (1945). Nonparametric Tests Against Trend. Econometrica, 13(3): 245-259.
 Salas, J.D. (1980). Applied modeling of hydrologic times series. Water Resources Publication, 484 pp.
 von Storch, V. H. (1995). Misuses of statistical analysis in climate research, In: Analysis of Climate Variability: Applications of Statistical Techniques, ed. von H. V. Storch and A. Navarra A. Springer-Verlag, Berlin: 11-26.
 Yue, S. and Wang, C. Y. (2002). Applicability of prewhitening to eliminate the influence of serial correlation on the Mann-Kendall test. Water Resources Research, 38(6), <doi:10.1029/2001WR000861>

Examples

```
x<-c(Nile)
pwmk(x)
```

 spear

Spearman's Rank Correlation Test

Description

Spearman's Rank Correlation test by Lehmann (1975) and Sneyers (1990) is useful in detecting trends.

Usage

```
spear(x)
```

Arguments

x - Time series data vector

Details

Spearman's Rank Correlation test by Lehmann (1975) and Sneyers (1990) is implemented in this function.

Value

Correlation coefficient - Spearman's Correlation coefficient value

Z-Transformed Test Statistic value - Z-transform value to test significance $\rho(\sqrt{n-1})$

References

Lehmann, E. L. (1975). Nonparametrics: statistical methods based on ranks. Holden-Day, Inc., California, 457 pp.

Sneyers, R. (1990). On the statistical analysis of series of observations. World Meteorological Organization, Technical Note no. 143, WMO no. 415, 192 pp.

Examples

```
x<-c(Nile)
spear(x)
```

tfpwmk

Mann-Kendall Trend Test Applied to Trend-Free Prewhitened Time Series Data in Presence of Serial Correlation Using Yue et al. (2002) Approach

Description

When the time series data are not random and influenced by autocorrelation, the trend component is removed from the data and is prewhitened prior to the application of the trend test.

Usage

```
tfpwmk(x)
```

Arguments

x - Time series data vector

Details

The linear trend component is removed from the original data and then prewhitened using the lag-1 serial correlation coefficient. The prewhitening data are then tested with Mann-Kendall trend test.

Value

Z-Value - Z statistic after trend-free prewhitening (TFPW)

Sen's Slope - Sen's slope for TFPW series

Old Sen's Slope - Sen's slope for original data series (x)

P-value - P-value after trend-free prewhitening

S - Mann-Kendall S statistic

Var(s) - Variance of S

Tau - Mann-Kendall's Tau

References

Kendall, M. (1975). Rank Correlation Methods. Griffin, London, 202 pp.

Kulkarni, A. and H. von Storch. 1995. Monte carlo experiments on the effects of serial correlation on the MannKendall test of trends. Meteorologische Zeitschrift N.F, 4(2): 82-85.

Mann, H. B. (1945). Nonparametric Tests Against Trend. Econometrica, 13(3): 245-259.

Salas, J.D. (1980). Applied modeling of hydrologic times series. Water Resources Publication, 484 pp.

Sen, P. K. (1968). Estimates of the Regression Coefficient Based on Kendall's Tau. Journal of the American Statistical Association, 63(324): 1379. <doi:10.2307/2285891>

von Storch, V. H. (1995). Misuses of statistical analysis in climate research, In: Analysis of Climate Variability: Applications of Statistical Techniques, ed. von H. V. Storch and A. Navarra A. Springer-Verlag, Berlin: 11-26.

Yue, S., Pilon, P., Phinney, B., and Cavadias, G. (2002). The influence of autocorrelation on the ability to detect trend in hydrological series. Hydrological Processes, 16(9): 1807–1829. <doi:10.1002/hyp.1095>

Examples

```
x<-c(Nile)
tfpwmk(x)
```

x

Annual flow of the Nile River

Description

Nile River data available with R base is used for testing purpose

Usage

x

Format

Nile river flow measured at Aswan station during 100 year period from 1871 to 1970 is used for testing

References

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Index

*** datasets**

x, [17](#)

bbsmk, [2](#)

bbssr, [3](#)

bcpw, [5](#)

mkttest, [6](#)

mmkh, [7](#)

mmkh3lag, [9](#)

mmky, [10](#)

mmky1lag, [11](#)

pbmk, [13](#)

pwmk, [14](#)

spear, [15](#)

tfpwmk, [16](#)

x, [17](#)